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Disodium Zincosilicate, Na₂ZnSi₃O₈

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The structure of synthetic Na₂ZnSi₃O₈ [monoclinic P2₁; a = 6.660 (6), b = 8.629 (6), c = 6.411 (8) Å, $\beta = 103.70$ (7)°; Z = 2, $D_m = 2.94$, $D_x = 2.95$ g cm⁻³] has been refined to R = 0.033 for 1077 independent reflexions from Mo Ka radiation. Corner-sharing [SiO₄] tetrahedra form chains with three tetrahedra in the identity period of the chain. These *Dreierketten* form tetrahedral layers $2[Si_3O_8]$. Together with $|ZnO_4|$ tetrahedra the [SiO₄] groups constitute a framework resembling that of paracelsian, BaAl₂Si₂O₈. The sodium ions occupy irregular cavities: Na(1) is seven-coordinated (mean bond length 2.718 Å) with two additional oxygens at 3.4 Å; Na(2) may be regarded as seven or eight-coordinated (mean bond lengths 2.529 or 2.600 Å). The structure of Na₂ZnSi₃O₈ shows remarkable similarities to the sodic plagioclase feldspars, (Na,Ca)-(Al,Si)₄O₈, and other framework aluminosilicates. The formula

$$Si-O = 1.571 - 0.068 \Delta Zn_{br} + 0.067 [\Sigma 1/(Na-O)^2] - 0.025/cos(T-O-T),$$

whose constants were derived by multiple linear regression analysis for feldspars and modified to account for the substitution of Zn for Al, gives an excellent estimation of the 12 individual Si–O bond lengths in this compound.

Introduction

Disodium zincosilicate, Na₂ZnSi₃O₈, was first described by Litvin, Mel'nikov, Ilyukhin & Nikitin (1965). In the present study single crystals were synthesized by heating a mixture of 5.0 g gel of composition Na₂O. ZnO. 3SiO₂. nH₂O [prepared by the method of Hamilton & Henderson (1968)] and 1.4 g pure SiO₂ (Riedel-de Haën) in sealed silver tubes for several days at 1 kbar and 450°C. Chemical, electron microprobe, and thermogravimetric analyses and IR spectra reveal a partial replacement of Na by H in agreement with the formula Na_{2-x}H_xZnSi₃O₈ with $x \le 0.25$.

The cell dimensions were obtained by a least-squares analysis of 19 peaks from a Guinier powder photograph (Cu K α radiation, $\lambda = 1.5418$ Å). Intensities of 1077 independent reflexions from a crystal of dimensions $0.08 \times 0.17 \times 0.22$ mm were collected from θ - 2θ scans on a Siemens four-circle diffractometer with Mo K α radiation ($\mu = 40.3$ cm⁻¹). Lorentz, polarization and absorption corrections were applied. From systematic absences of 0k0 reflexions with k = 2n + 1and an N(z) test (Howells, Phillips & Rogers, 1950) the space group $P2_1$ was deduced.

Approximate atomic coordinates were determined from a three-dimensional Patterson synthesis and were refined by least-squares and Fourier methods with scattering factors for half-ionized atoms. For the final coordinates in Table 1 the unweighted residual, using all

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Table 1. Fractional atomic coordinates and thermal parameters with estimated standard deviations in parentheses

Atomic coordinates and anisotropic thermal parameters have been multiplied by 10⁴. The origin is fixed by *v* for the zinc atom. $T = \exp[-(h^2B_{11} + k^2B_{22} + l^2B_{33} + 2hkB_{12} + 2hlB_{13} + 2klB_{23})].$

	χ.	v	Ζ	$B_{\rm iso}$ (Å ²)	<i>B</i> ₁₁	B 22	B ₃₃	<i>B</i> ₁₂	B ₁₃	B ₂₃
Na(1)	4673 (7)	8764 (6)	847 (7)	1.92(7)	111 (7)	85 (5)	108 (8)	-29(5)	12 (6)	12 (5)
Na(2)	2155(6)	4337 (5)	3297 (6)	1.02(6)	58 (6)	31 (3)	84 (7)	8 (4)	12 (5)	! (4)
Zn	6070(1)	2428 (1)	4646(1)	0.50(1)	25(1)	17(1)	48(1)	3 (1)	8 (1)	3 (1)
Si(1)	2660 (3)	746 (3)	6440 (3)	0.40(3)	18 (3)	13 (2)	44 (3)	2 (2)	5 (3)	0 (2)
Si(2)	-1038(3)	568 (3)	-7508 (3)	0.40(3)	25 (3)	12(2)	35 (3)	2 (2)	5 (3)	0(2)
Si(3)	127 (3)	2391 (4)	9067 (3)	0.39(3)	22 (3)	14 (2)	35 (3)	0(3)	3 (2)	-1(3)
O(1)	5729 (9)	4352 (8)	2965 (9)	0.68(9)	33 (9)	11 (5)	82 (11)	-7(6)	8 (8)	7 (6)
O(2)	6691 (10)	830 (9)	2817(10)	0.90(9)	38 (9)	30 (6)	92 (11)	-2(7)	18 (8)	-20 (7)
$\vec{O}(\vec{3})$	3509 (8)	2297 (9)	5606 (9)	0.78(8)	28 (8)	17 (5)	94 (10)	-4(7)	19(7)	10 (8)
O(4)	7935(9)	2247(9)	7478 (9)	0.81(9)	41 (8)	31 (6)	66 (10)	-9(7)	-8(7)	-1(7)
O(5)	8874 (9)	-862(8)	798 (9)	0.71(9)	50 (10)	15 (5)	55 (10)	9(6)	4 (8)	-7(7)
0(6)	546 (9)	109 (8)	4755 (10)	0.71(9)	38 (9)	24 (6)	54 (10)	-12(6)	-4(8)	2 (6)
O(7)	1848 (10)	1173 (8)	8630 (10)	0.83(9)	51 (10)	32 (6)	60 (11)	13 (6)	19 (8)	1 (7)
O(8)	-70(9)	2075 (7)	-8476 (9)	0.68 (9)	49 (9)	17 (6)	52 (10)	6 (5)	17(7)	4 (6)

Table 2. Interatomic distances (Å) and valence angles (°) in $Na_2ZnSi_3O_8$

O^b: oxygen atom bonded to two silicon atoms (bridging oxygen atom); all other oxygens are bonded to one silicon and one zinc atom.

[SiO₄] tetrahedra						
•	Si-O dis	tances			$\mathbf{O}\cdots\mathbf{O}$	O–Si–O
	Observed	Predicted	⊿Zn _{br}		distances	angles
$S_{i}(1) = O(1)$	1.597 (7)	1.607	0.5	O(1)O(3)	2.708 (10)	116-2 (4)
$S_{i}(1) = O(3)$	1.594 (8)	1.603	0.5	$O(1) - O(6)^{b}$	2.646 (9)	109.0 (4)
$S_i(1) = O(6)^b$	1.653(7)	1.648	-0.5	$O(1) - O(7)^{b}$	2.627(10)	107.5 (4)
$S_{i}(1) = O(7)^{b}$	1.661(8)	1.650	-0.5	$O(3) - O(6)^{b}$	2.693 (10)	112.0 (4)
Mean	1.626	1.629		$O(3) - O(7)^{b}$	2.634 (10)	108.0 (4)
mean	1 020	1 02/		$O(6)^{b} - O(7)^{b}$	2.598 (9)	103 2 (3)
				Mean	2.651	109.3
S:(2) (2)	1.501(7)	1.587	0.75	$O(2) - O(5)^{b}$	2.610(10)	108.0(4)
$S(2) = O(2)^{b}$	1.636(7)	1.642	-0.25	$O(2) - O(6)^{b}$	2.648 (9)	110.7(4)
S(2) = O(3) $S(2) = O(6)^{b}$	1.628(7)	1.631	-0.25	$O(2) - O(8)^{b}$	2.709 (10)	114 · 1 (4)
$S_{1}(2) = O(0)$ $S_{2}(2) = O(8)^{b}$	1.637(7)	1.638	-0.25	$O(5)^{b} - O(6)^{b}$	2.653 (9)	108.8(4)
Mean	1.623	1.624		$O(5)^{b} - O(8)^{b}$	2.642 (9)	107.6 (4)
Weath	1 025			$O(6)^{b} - O(8)^{b}$	2.634 (9)	107 • 6 (4)
				Mean	2.649	109.5
$S_{i}(3) = O(4)$	1.575 (6)	1.568	0.75	$O(4) - O(5)^{b}$	2.700 (9)	114 1 (4)
S(3) = O(4) $S(3) = O(5)^{0}$	1.642 (8)	1.642	-0.25	$O(4) - O(7)^{b}$	2.699 (9)	114 · 9 (4)
S(3) = O(3) $S(3) = O(7)^{b}$	1.627(7)	1.633	-0.25	$O(4) - O(8)^{b}$	2.627 (9)	109 · 7 (4)
$S_{1}(3) = O(8)^{b}$	1.634(8)	1.638	-0.25	$O(5)^{b} - O(7)^{b}$	2.645 (10)	108.0(4)
Mean	1.620	1.622		$O(5)^{b} - O(8)^{b}$	2.525 (9)	103 · 1 (3)
Mean	1 020			$O(7)^{b} - O(8)^{b}$	2.611 (10)	106 2 (4)
				Mean	2.635	109-3
[ZnO ₄] tetrahedron						
	Zn–O	distances			$\mathbf{O} \cdot \cdot \cdot \mathbf{O}$	O-Zn-O
	Observed	Predicted	∆Zn _{br}		distances	angles
$Z_n = O(1)$	1.963 (7)	1.963	0	O(1)O(2)	3.112(10)	106.6(3)
$Z_{n-O(2)}$	1.918 (7)	1.961	0	O(1)-O(3)	3.063(10)	103-1 (3)
$Z_n - O(3)$	1.949 (6)	1.960	0	O(1)–O(4)	3-437 (10)	123.0(3)
Zn-O(4)	1.948 (6)	1.941	0	O(2)–O(3)	3 · 329 (10)	118-9(3)
Mean	1.945	1.95		O(2)–O(4)	3.153 (10)	109 3 (3)
				O(3)–O(4)	2.908 (8)	96 - 5 (3)
				Mean	3.167	109-6

Table 2. (cont.)

T-O-T	angles	Summary of mean angles		
Si(1) - O(6) - Si(2)	140.6 (5)	and distances		
Si(1) - O(7) - Si(3)	$132 \cdot 2(4)$	Mean Si–O ^b	1.640	
Si(2) - O(5) - Si(3)	135-0 (4)	Mean Si–O	1.589	
Si(2) - O(8) - Si(3)	128.8(4)	Grand mean Si-O	1.623	
Mean	134-2	Grand mean Zn–O	1.945	
		Grand mean O · · · O		
Zn-O(1)-Si(1)	121.5 (3)	Si tetrahedra	2.645	
Zn = O(2) = Si(2)	$122 \cdot 1(4)$	Zn tetrahedron	3.167	
Zn-O(3)-Si(1)	124.1 (4)	Mean O-Si-O	116.2	
Zn-O(4)-Si(3)	152.3 (4)	Mean $O-Si-O^b$	110.9	
Mean	130.0	Mean O^b -Si- O^b	106-4	
		Grand mean $O-T-O$		
		Si tetrahedra	109-4	
		Zn tetrahedron	109.6	
Na polyhedra				
Na-O dista	nces	Na-O distances		
Na(1)–O(2)	2.403 (9)	Na(2)—O(3)	2 · 339 (8	
-O(1)	2.448 (8)	O(1)	2 440 (8	
-O(4)	2.602(9)	-O(6)	2 510 (9	
-O(3)	2.634 (8)	-O(8)	2 550 (7	
-O(5)	2.824(8)	-O(5)	2 557 (8	
-O(7)	2.934 (8)	-O(4)	2.558 (9	
-O(7')	3.180(8)	$-\mathbf{O}(2)$	2.748 (8	
-O(8)	3.410(8)	$-\mathbf{O}(7)$	3.096 (7	
-O(2')	3 427 (8)	Mean $(CN = 7)$	2.529	
Mean ($CN = 7$)	2.718	Mean $(CN = 8)$	2.600	
Mean $(CN = 9)$	2.874	、		

reflexions, is R = 0.048 for the isotropic refinement and 0.033 for the anisotropic (Hesse, 1972).* Bond lengths and valence angles are listed in Table 2.

* A list of structure factors has been deposited with the British Library Lending Division as Supplementary Publication No. SUP 32226 (11 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 13 White Friars, Chester CH1 1NZ, England.

Discussion of the structure

A short description of this structure was given at the 1973 Annual Meeting of the Deutsche Mineralogische Gesellschaft in Frank furt/Main (Hesse & Liebau, 1974). It is in fair agreement with the result of an independent structure analysis of $Na_2ZnSi_3O_8$ by Plakhov, Simonov & Belov (1974).



Fig. 1. Comparison between the structures of (a) $Na_2ZnSi_3O_8$ and (b) paracelsian $BaAl_2Si_2O_8$. Only one of the two tetrahedral layers per unit cell has been shown for each structure. $[SiO_4]$ and $[(Si,Al)O_4]$ tetrahedra are shown black, $[ZnO_4]$ tetrahedra white. Heavy circles are sodium and barium ions above the layers, light circles are those below.

In $Na_2ZnSi_3O_8$ the $[SiO_4]$ tetrahedra are cornershared to form chains parallel to [001] containing three tetrahedra in their repeat unit (Dreiereinfachketten: Liebau, 1972). These chains are linked to Dreiereinfachschichten of composition $2[Si_3O_8]$ parallel to (100) (Fig. 1 of Plakhov, Simonov & Belov, 1974). The nonbridging O atoms of the silicate layers are bonded to tetrahedral Zn oxyanions so that $[SiO_4]$ and $[ZnO_4]$ tetrahedra form a three-dimensional framework. Na₂ZnSi₃O₈ is an ordered tektozincosilicate, as evidenced by the mean Si-O bond lengths (Table 1) which are similar to those found in ordered paracelsian-type structures [1.623 and 1.624 Å in SrAl₂Si₂O₈ (Griffen, Ribbe & Gibbs, 1977) and 1.616 and 1.622 Å in BaAl₂Si₂O₈ (Craig, Louisnathan & Gibbs, 1973)]. The topology of this framework is similar to that in paracelsian, BaAl₂Si₂O₈, (Smith, 1953) with the sodium zincosilicate-to-paracelsian transformation matrix $101/\overline{101}/010$ (Fig. 1). The Na⁺ ions fill cavities within the framework resulting in irregular coordination polyhedra of seven O atoms at less than 3.19 Å and two more at 3.4 Å for Na(1) and eight at less than 3.10 Å for Na(2). It is interesting that the isotropic temperature factors of 1 9 and 1 0 Å² correspond to mean ^[VII]Na–O bond lengths of 2.718 and 2.529 Å, respectively, for Na(1) and Na(2); the larger temperature factor may be due in part to H replacing Na in the Na(1) site.

Discussion of the bonding

There are a number of Na-containing compounds – NaAlSi₃O₈ (the plagioclase feldspar mineral albite), NaAlSi₂O₆.H₂O (the zeolite analcime), and Na₂(OH)AlSi₃O₈ (ussingite) – which share structural



Fig. 2. A plot of the observed T-O distances versus those calculated from the regression equation for Na₃ZnSi₃O₈.

similarities with $Na_2ZnSi_3O_8$. Albite and analcime are like $Na_2ZnSi_3O_8$ in that every O atom (excluding water molecules) is bonded to two tetrahedrally coordinated (*T*) cations, forming an infinite three-dimensional framework, but ussingite has an 'interrupted' framework (Rossi, Tazzoli & Ungaretti, 1974).

Phillips & Ribbe (1973) applied multiple linear regression analysis to the geometric and chemical variables in sodic plagioclase feldspars (Na_x-Ca_{1-x}Al_{2-x}Si_{2+x}O₈: $0 \le x \le 0.3$) in order to determine their relative effects on individual *T*-O bond lengths. They showed that *T*-O bond lengths in all the aforementioned compounds could be predicted with correlation coefficients of 0.99. Thus, to determine if the bonding effects observed in these Na-rich aluminosilicates are similar to those in Na₂ZnSi₃O₈, we have slightly modified Phillips & Ribbe's (1973, p. 337) regression equation to account for the substitution of tetrahedral Zn for Al in the structural framework. We have estimated the 12 individual Si-O bond lengths

Si-O =
$$1.571 - 0.068 \Delta Z n_{br} + 0.067 [\Sigma 1/(Na-O)^2] - 0.025/cos(T-O-T),$$

where $\Delta Zn_{br} \equiv Zn_{br} - \langle Zn_{br} \rangle$, and the term Zn_{br} represents the Zn content of the tetrahedron adjoining the individual Si–O distance under consideration, and $\langle Zn_{br} \rangle$ is the mean content of all four tetrahedra adjacent to the tetrahedron under consideration. Values of ΔZn_{br} are listed in Table 2; those which are positive and non-zero are associated with bonds to Si from O atoms which are also bonded to Zn.

The ΔZn_{br} term in the equation accounts for what might be called a 'linkage effect'. In Na₂ZnSi₃O₈ the Si $-O(\rightarrow Zn)$ bonds (given in italics in Table 2) are 0.051 Å shorter on average than the Si–O(\rightarrow Si) bonds. The second term in the equation accounts for the Coulombic interaction of the Na cation(s) with the O in an individual Si-O bond. Coordination-number effects are considered by summing over all Na-O bonds to that oxygen. Note that Si-O bonds to three coordination O atoms in this structure are 0.034 Å longer on average than those of four-coordinated O atoms. As documented in many previous studies of compounds containing polymerized tetrahedra (e.g. Louisnathan & Gibbs, 1972*a*,*b*), the T–O distances involved in wide T–O–T angles tend to be shorter than those involved in narrow T-O-T angles, regardless of the chemical identity of the T atoms or the degree of polymerization. The last term in the equation accounts for this effect, and it is expressed as the inverse cosine of the T-O-T angle in order to best linearize the relation to T-O distances (Gibbs, Hamil, Louisnathan, Bartell & Yow, 1972). Values predicted from this equation are listed in Table 2 and plotted in Fig. 2. The correlation coefficient for the estimated and observed Si-O distances, which range from 1.575 to 1.661 Å, is r = 0.97. The leastsquares line of best fit $(Si-O)_{est} = 0.94(Si-O)_{obs} + 0.09$ is statistically the same as the expected 45° line. We regard this as evidence of the correctness of the bonding model proposed for Na₂ZnSi₃O₈.* Zn-O bonds may be predicted reasonably well by adding to the intercept the difference between the mean Zn-O and Si-O distances (1.945 - 1.623 = 0.322 Å).

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* A reviewer has pointed out that the equation $Si-O = 1.623 - 0.055 \Delta Zn_{br}$ estimates Si-O slightly better than the more general equation derived and used successfully by Phillips & Ribbe (1973) and Ribbe (1974) for the aluminosilicates. This indicates that ΔZn_{br} can be considered to be the preponderant factor in the analysis of bonding effects in $Na_2ZnSi_3O_8$, although this may not be the case in other framework structures. For example, in Na_2ZnSi_4 (Plakhov, Simonov, Egorov-Tismenko & Belov, 1976) [ZnO₄] and [SiO₄] tetrahedra alternate in the framework, and therefore ΔZn_{br} is zero for all Si-O bonds. Our model predicts Si-O bond lengths of 1.645, 1.636, 1.645, 1.636 Å. The longer Si-O bond lengths are those to O atoms coordinated by three Na atoms, the shorter to those coordinated by only two Na.

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A Neutron Diffraction Study of Anhydrous Ethylenediamine D-Tartrate

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 $C_6H_{14}N_2O_6$, monoclinic, $P2_1$, a = 8.974 (5), b = 8.797 (5), c = 5.984 (4) Å, $\beta = 105.40$ (10)°, Z = 2, $\rho_{obs} = 1.52$ (1), $\rho_{calc} = 1.533$ (3) g cm⁻³. Neutron diffraction was used to locate precisely all the H atoms. The structure consists of diprotonated ethylenediamine cations and tartrate anions with extensive interionic hydrogen bonding and a weak intraionic hydrogen bond between a tartrate -OH and $-COO^-$ group [O-H = 0.956 (6) Å and $H \cdots O = 2.138$ (8) Å]. The shortest hydrogen bonds are from amine H atoms to carboxyl O atoms $[H(21)\cdots O(2) = 1.74$ (1) and $H(20)\cdots O(1) = 1.74$ (1) Å]. A comparison with Dtartaric acid is presented.

Experimental

The crystal was provided by G. K. Johnson and was prepared by slow evaporation at room temperature of a one-to-one aqueous mixture of ethylenediamine and D-tartaric acid. Only the anhydrous form was obtained. The crystal used for this study was bounded by ten faces and had axial dimensions of about $0.30 \times 0.40 \times 0.15$ cm. The neutron data were collected on a Mitsubishi Diffractometer equipped with a full circle, designed and built by the Department of Physics, University of Missouri– Columbia, machine shop, and interfaced to a PDP-11 computer at the University of Missouri Research Reactor. The data were collected by the θ -2 θ step-scan technique. With 25 carefully centered reflections, for